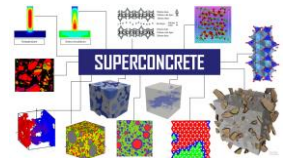


Elastic analysis of (concrete) plates on grade

Annex: Two relevant examples

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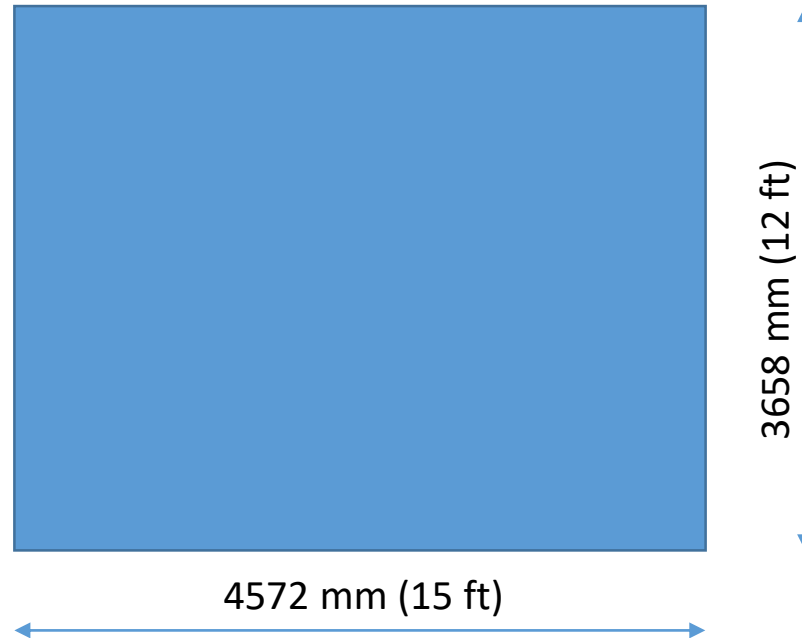
Overview

Two relevant cases:

Case #1: Center point load and positive ΔT (mid-day on sunny days)

Case #2: Point loads near corners and negative ΔT (mid-day on sunny days)

$$k_0 = 0.04073 \text{ N/mm}^3 \\ = 150 \text{ psi/in}$$

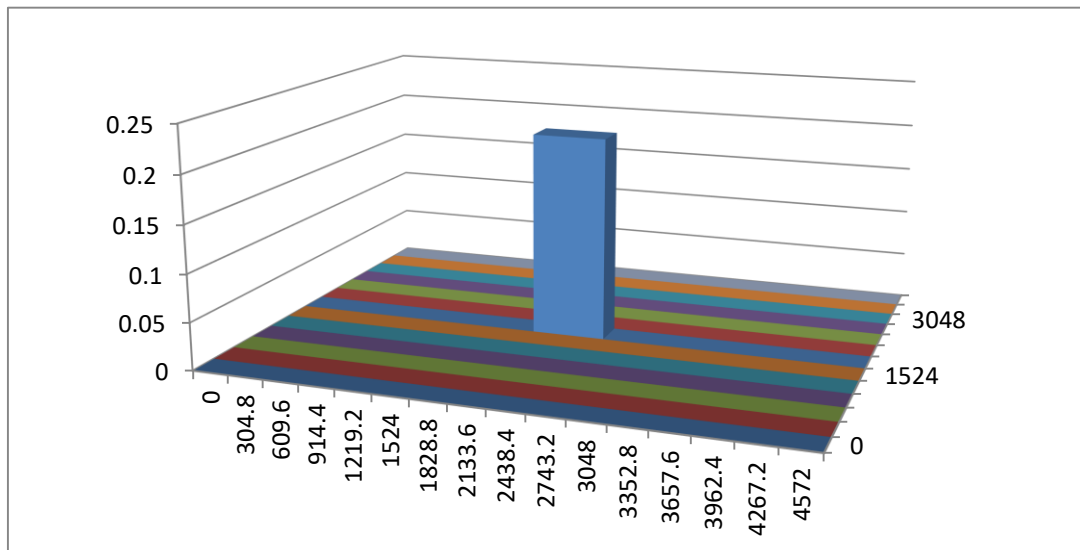


$$\Delta = \Delta x = \Delta y = 304.8 \text{ mm} \\ (1 \text{ ft})$$

Case #1

Point load: assumptions

0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0.215	0.215	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0



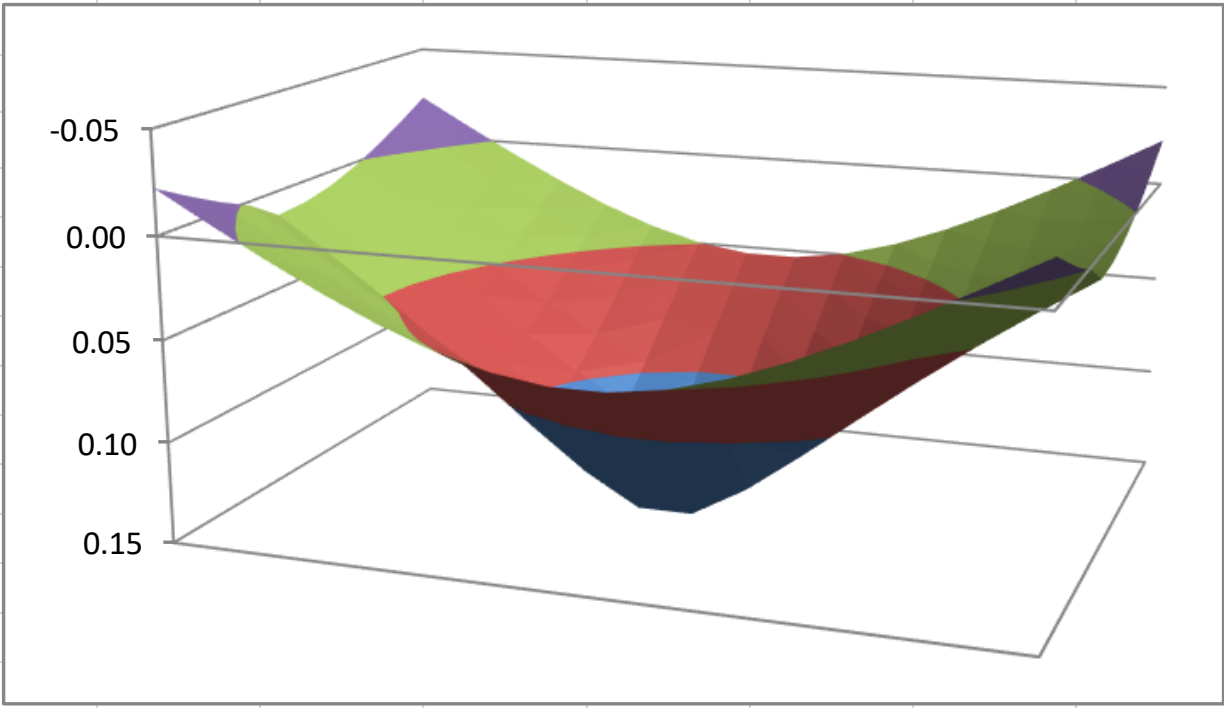
Due to symmetry reasons, the point load ($P=40$ kN) is distributed over 2 nodes/celles:

$$q_{P,eq} = \frac{P}{2 \cdot \Delta} = 0.215 \text{ N} / \text{mm}^2$$

Case #1

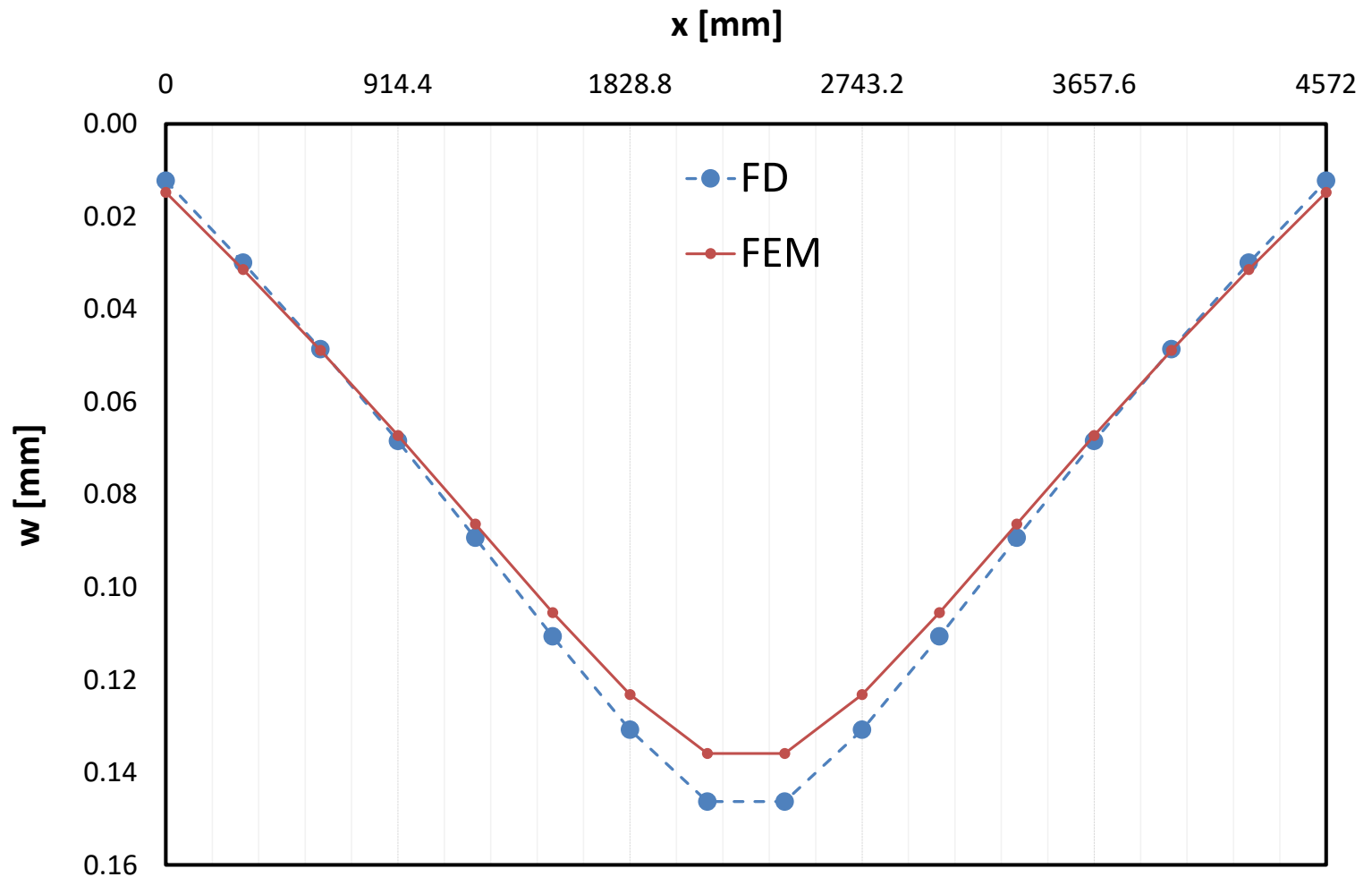
Point load: displacement field

E=	27586	MPa	Self-weight multiplier			Center-point force			Thermal effects	
s=	250	mm	γ_g =	0.00		F=	40.00	kN	Δt =	0
v=	0.2		g=	6.25	kN/m ²				α_c =	1.20E-05
γ =	25.0	kN/m ³							χ^* =	0.00E+00
D=	3.742E+10	Nmm								
k_0 =	0.04073	N/mm ³								
L_x =	5000	mm								
L_y =	5000	mm								
n=	10									
Δ =	304.8	mm								



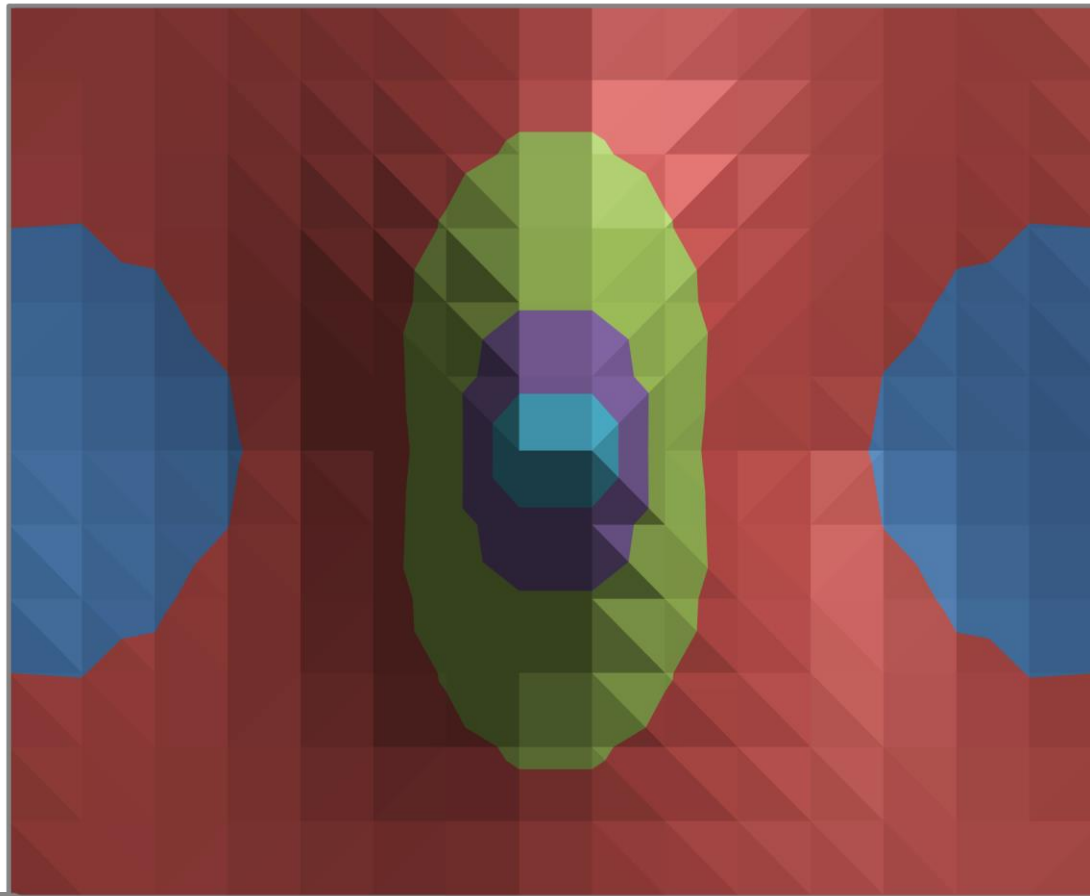
Case #1

Point load: displacement field (FD/FEM comparison)



Case #1

Point load: bending moments M_x

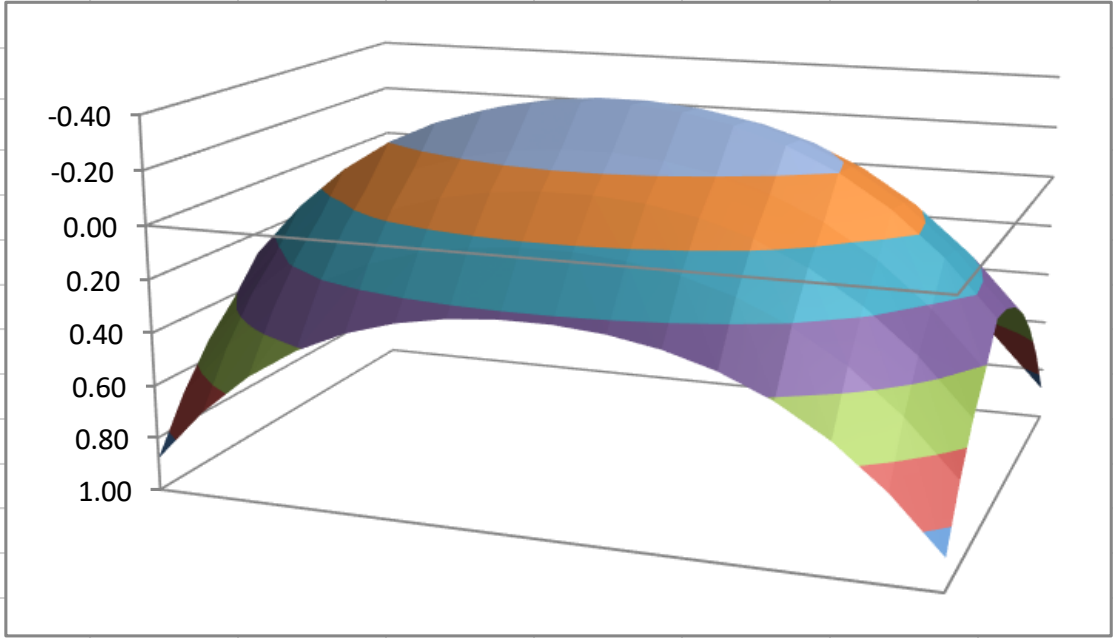


$M_{x,max} = 7764.33$ Nmm/mm

Case #1

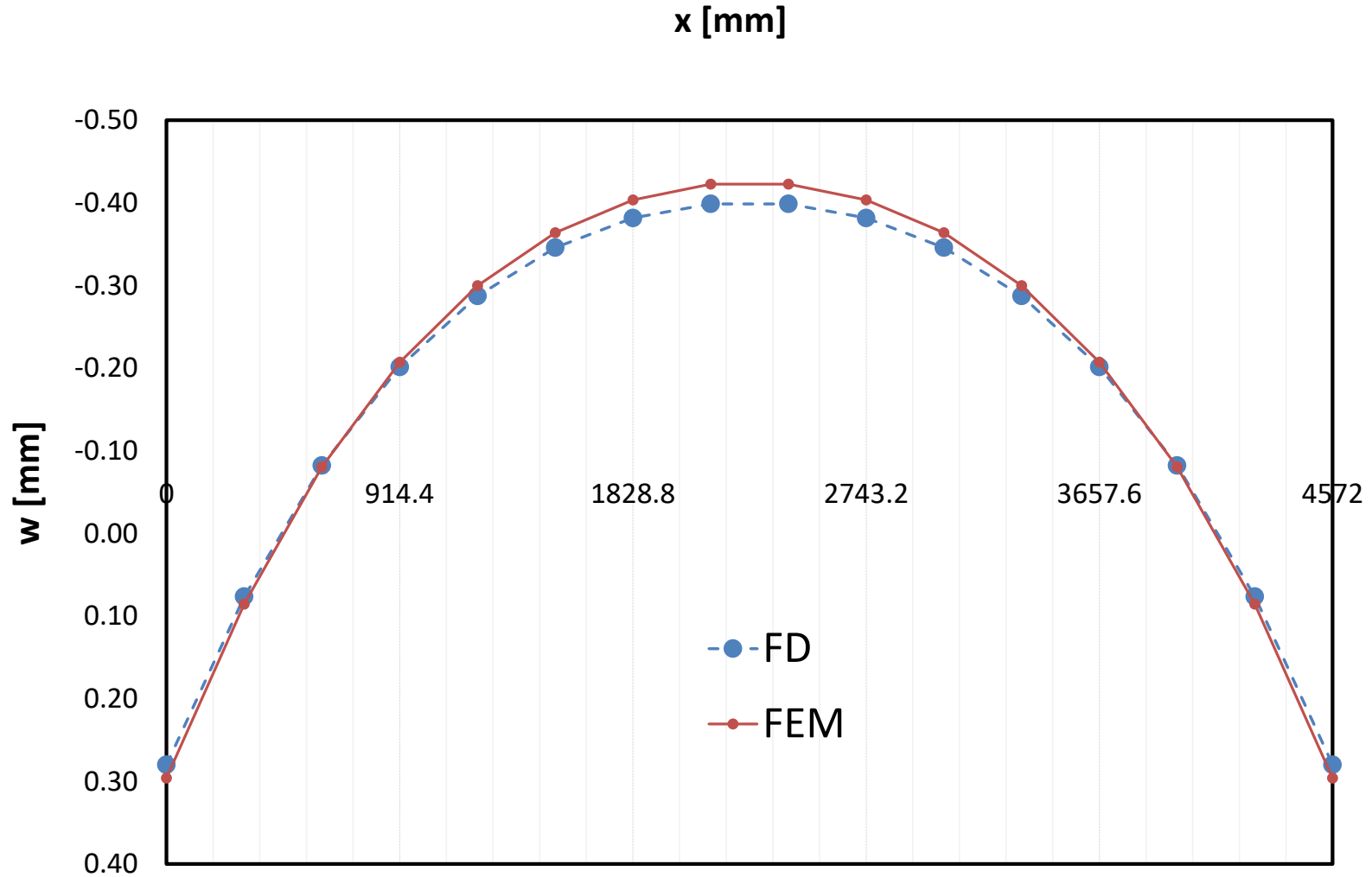
Thermal effects: displacement field

E=	27586	MPa	Self-weight multiplier			Center-point force			Thermal effects		
s=	250	mm	γ_g =	0.00		F=	0.00	kN	Δt =	10	°C
v=	0.2		g=	6.25	kN/m ²				α_c =	1.20E-05	°C ⁻¹
γ =	25.0	kN/m ³							χ^* =	-4.80E-07	mm ⁻¹
D=	3.742E+10	Nmm									
k_0 =	0.04073	N/mm ³									
L_x =	5000	mm									
L_y =	5000	mm									
n=	10										
Δ =	304.8	mm									



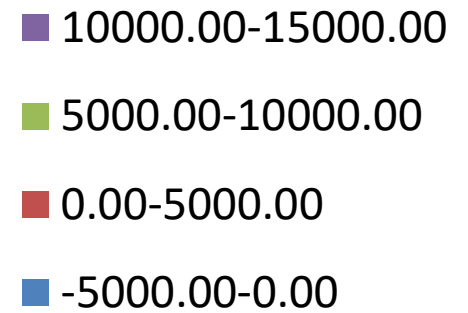
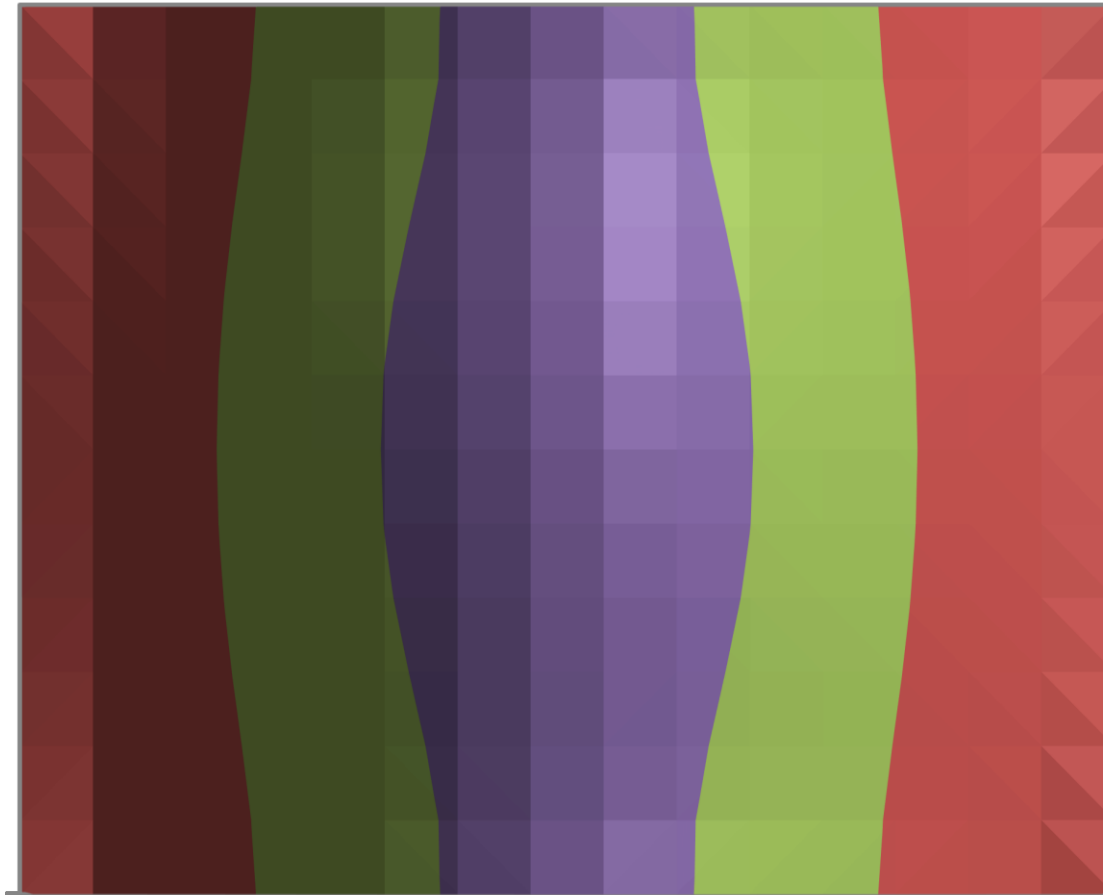
Case #1

Thermal effects: displacement field (FD/FEM comparison)



Case #1

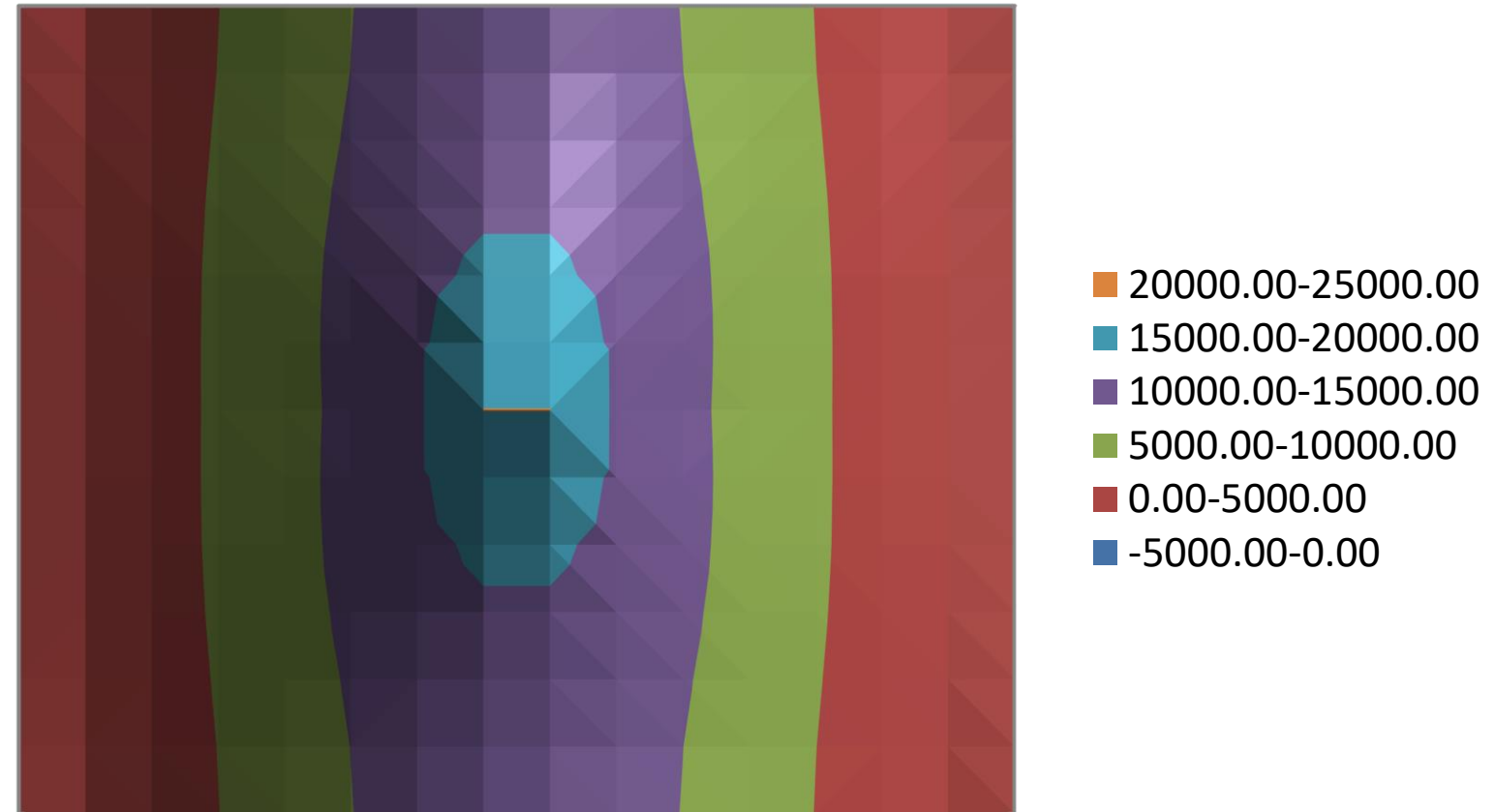
Thermal effects: bending moments M_x



$M_{x,max} = 12288.99$ Nmm/mm

Case #1

Thermal effects: maximum tensile stresses σ_x

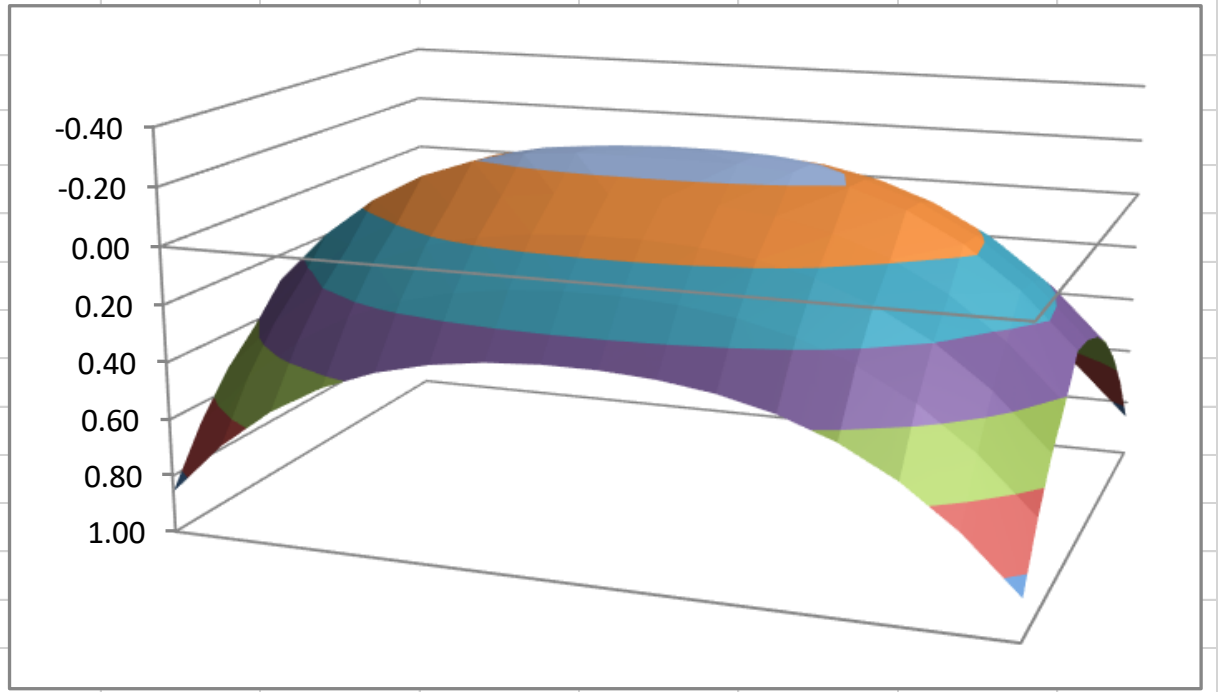


$$\sigma_{s,\max} = \frac{6 \cdot M_{x,\max}}{s^2} = \frac{6 \cdot (7764.33 + 12288.99)}{250^2} = 1.92 \text{ MPa}$$

Case #1

Load Combination: displacements

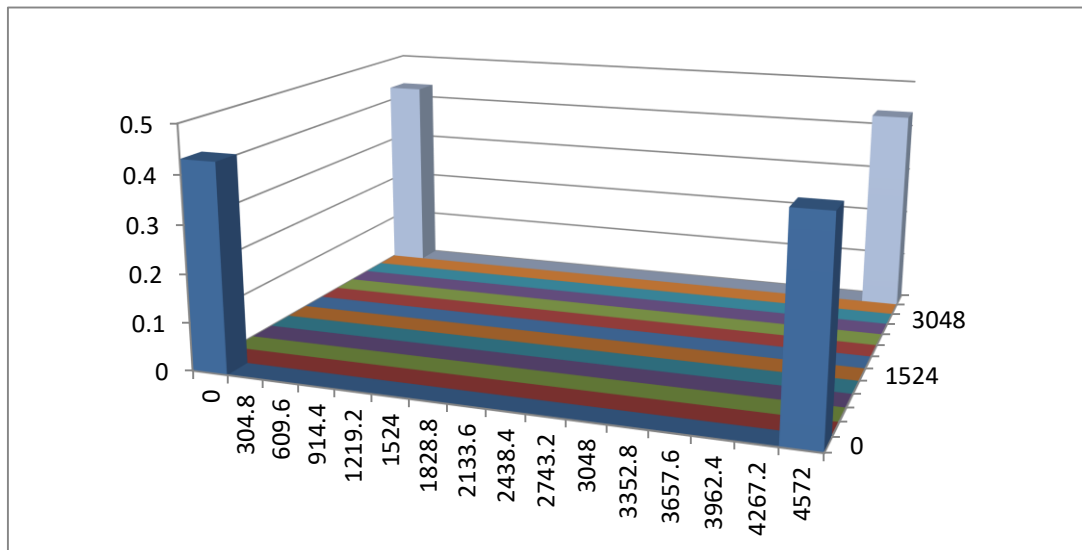
E=	27586	MPa	Self-weight multiplier			Center-point force			Thermal effects	
s=	250	mm	$\gamma_g=$	1.00		F=	40.00	kN	$\Delta t=$	10
v=	0.2		g=	6.25	kN/m ²				$\alpha_c=$	1.20E-05
$\gamma=$	25.0	kN/m ³							$\chi^*=$	-4.80E-07
D=	3.742E+10	Nmm								
$k_0=$	0.04073	N/mm ³								
$L_x=$	5000	mm								
$L_y=$	5000	mm								
n=	10									
$\Delta=$	304.8	mm								



Case #2

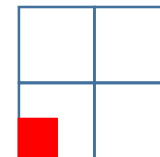
Point load: assumptions

0.430556	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.430556
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0.430556	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.430556



The point load ($P=40$ kN) is distributed over 1 node/cell close to the corners:

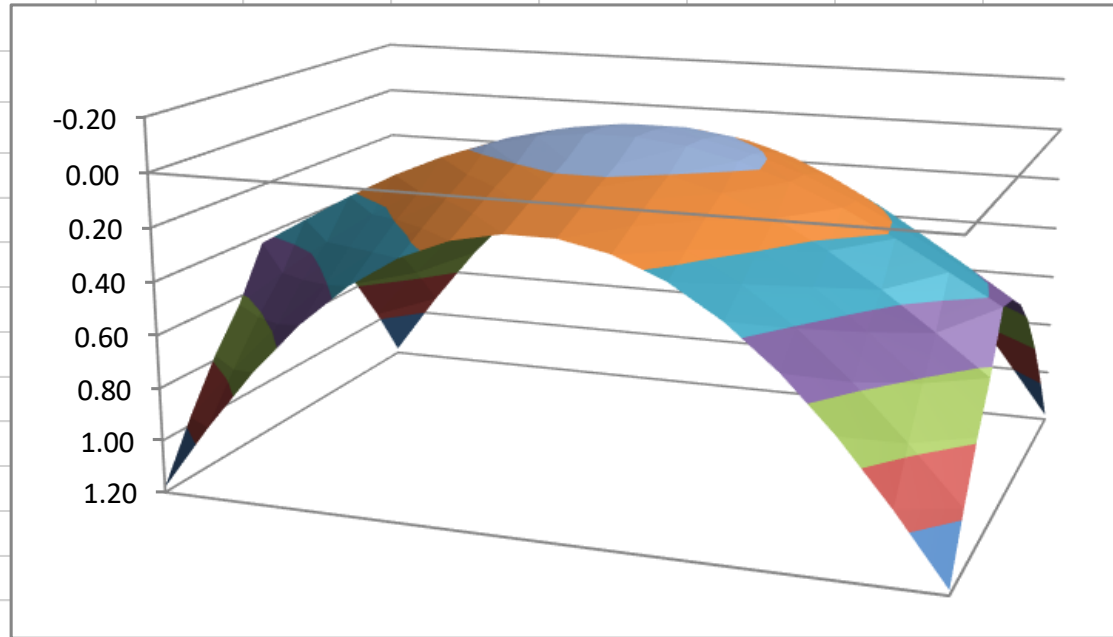
$$q_{P,eq} = \frac{P}{(\Delta/2)^2} = 1.722 \text{ N/mm}^2$$



Case #2

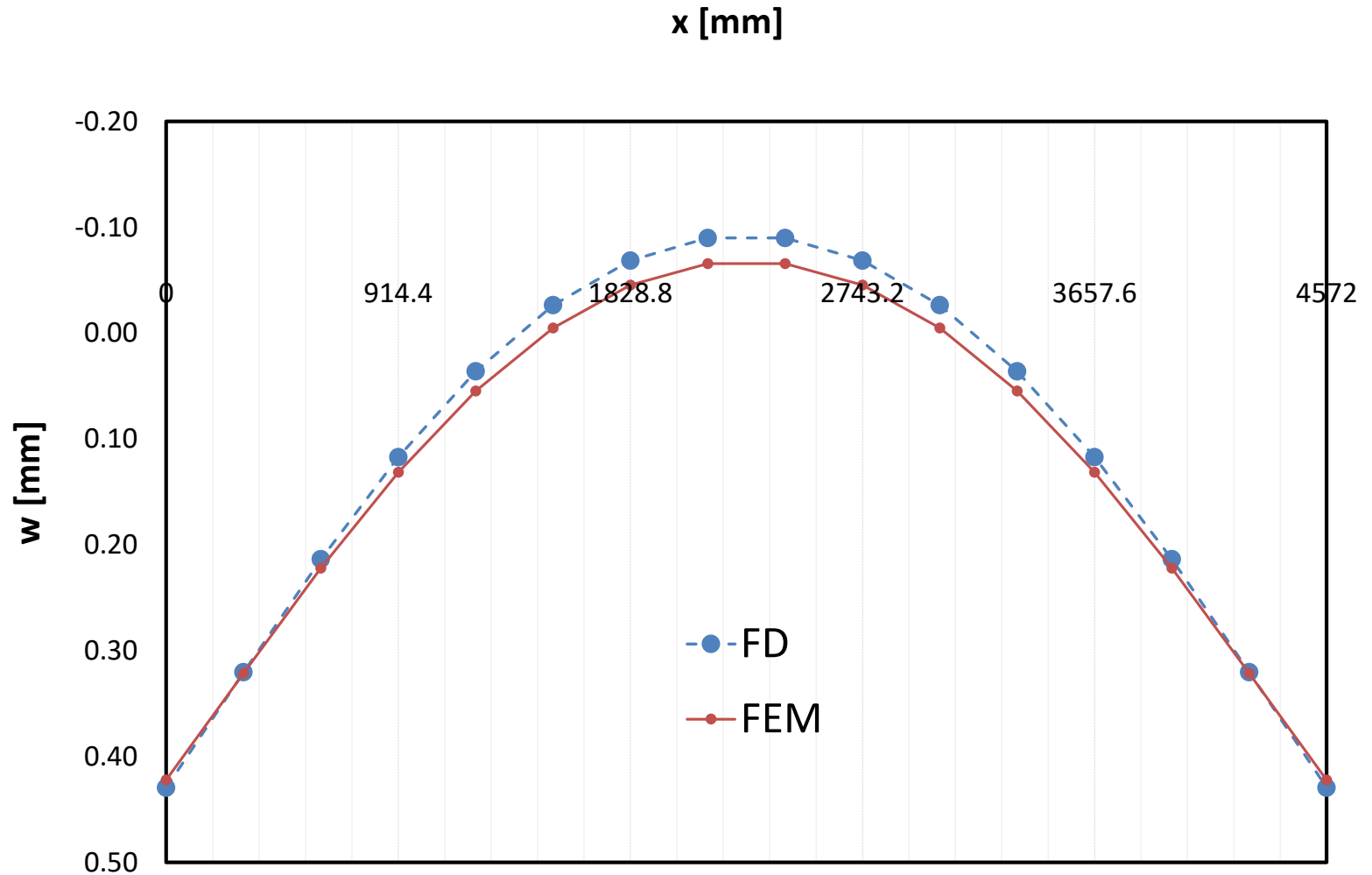
Point loads: displacement field

E=	27586	MPa	Self-weight multiplier			Center-point force			Thermal effects		
s=	250	mm	γ_g =	0.00		F=	40.00	kN	Δt =	0	°C
v=	0.2		g=	6.25	kN/m ²				α_c =	1.20E-05	°C ⁻¹
γ =	25.0	kN/m ³							χ^* =	0.00E+00	mm ⁻¹
D=	3.742E+10	Nmm									
k_0 =	0.04073	N/mm ³									
L_x =	5000	mm									
L_y =	5000	mm									
n=	10										
Δ =	304.8	mm									



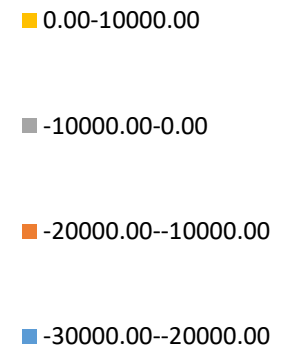
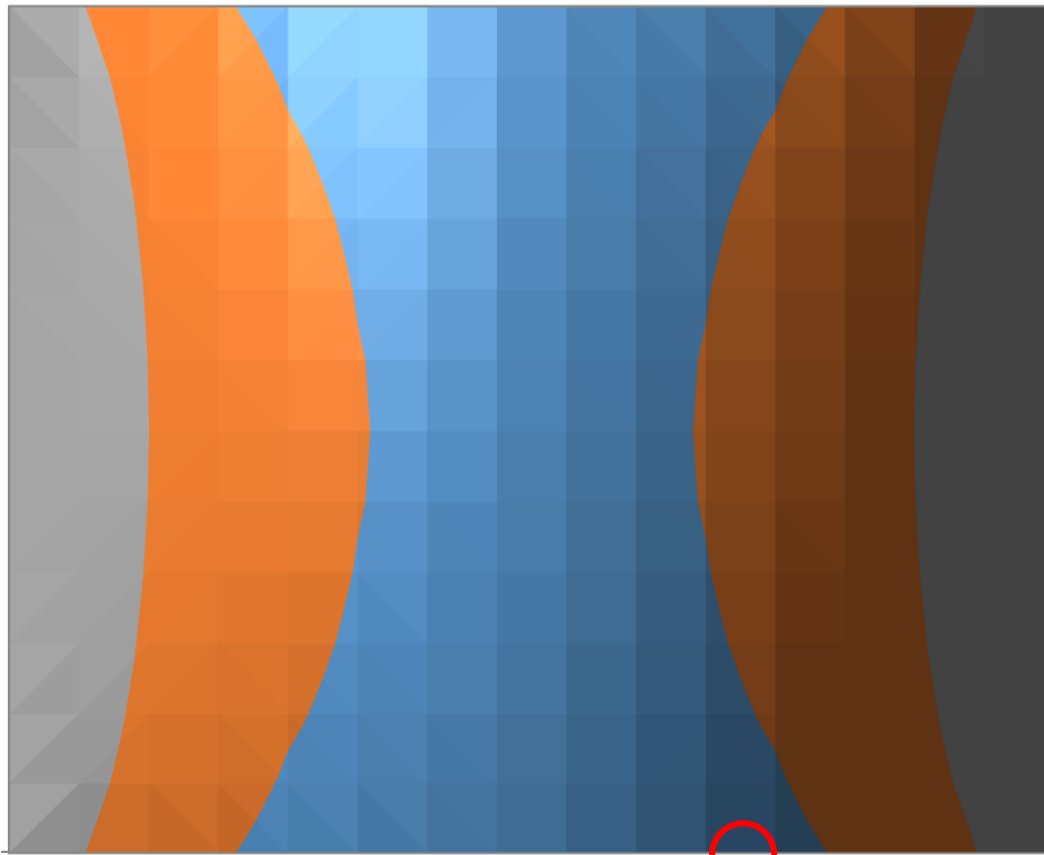
Case #2

Point loads: displacement field (FD/FEM comparison)



Case #2

Point loads bending moments M_x

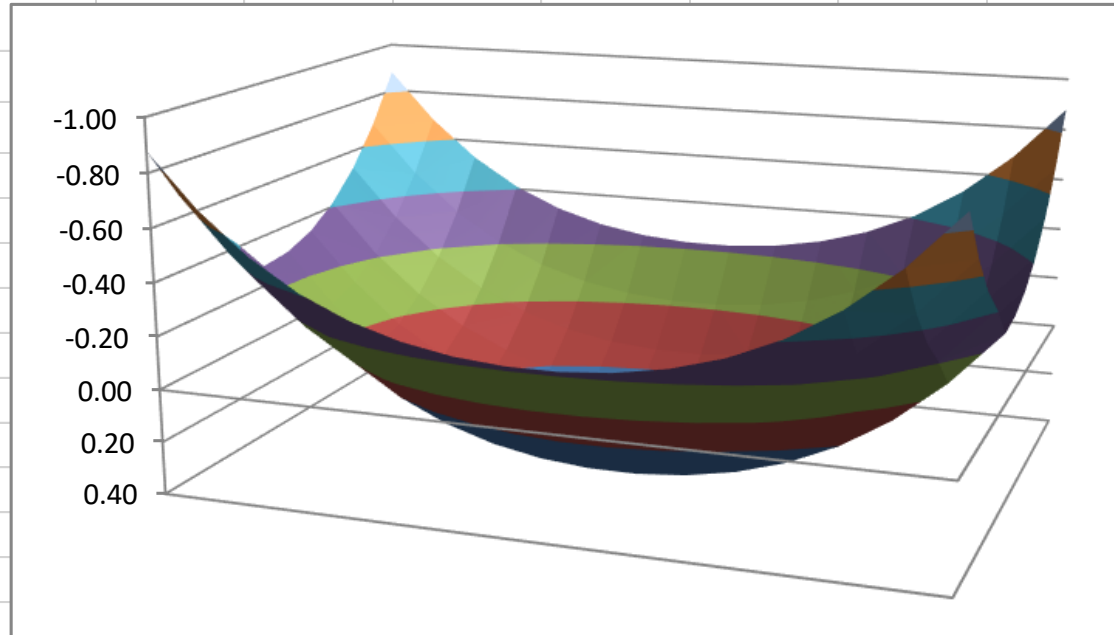


$M_{x,max} = 15249.12 \text{ Nmm/mm}$

Case #2

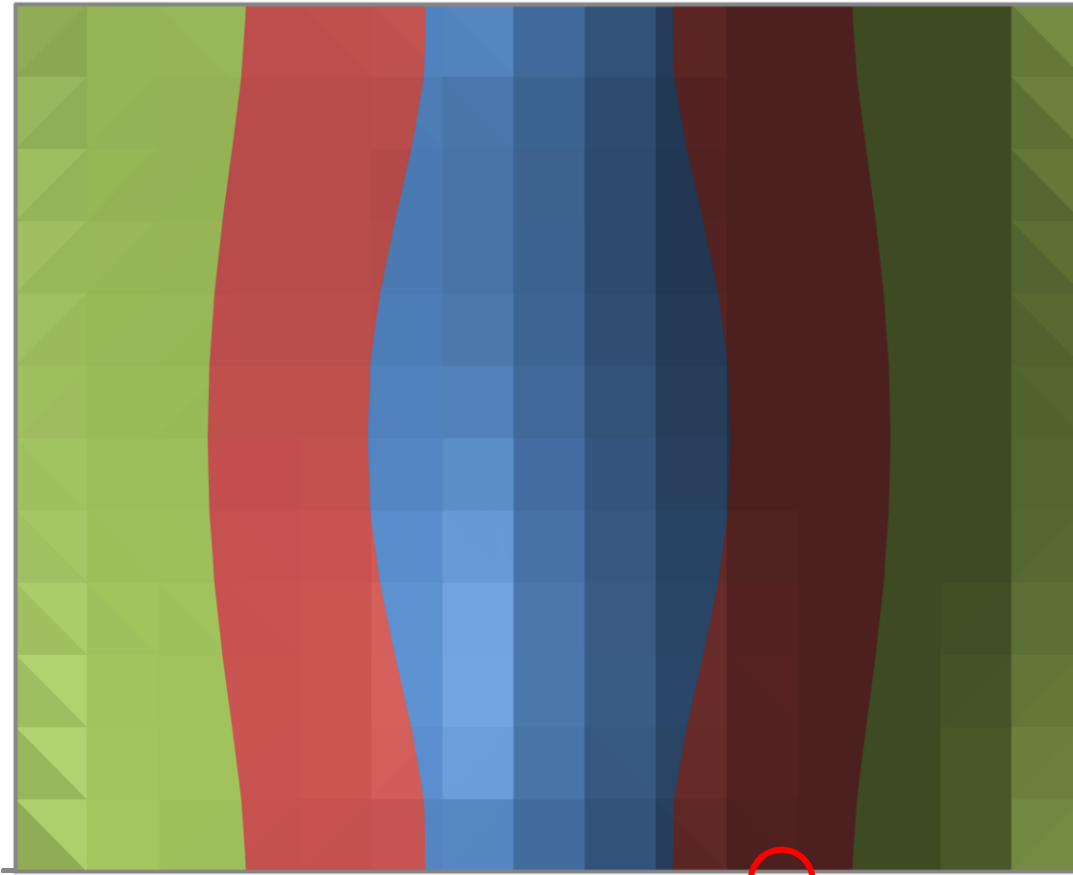
Thermal effects: displacement field

E=	27586	MPa	Self-weight multiplier			Center-point force			Thermal effects		
s=	250	mm	γ_g =	0.00		F=	0.00	kN	Δt =	-10	°C
v=	0.2		g=	6.25	kN/m ²				α_c =	1.20E-05	°C ⁻¹
γ =	25.0	kN/m ³							χ^* =	4.80E-07	mm ⁻¹
D=	3.742E+10	Nmm									
k_0 =	0.04073	N/mm ³									
L_x =	5000	mm									
L_y =	5000	mm									
n=	10										
Δ =	304.8	mm									



Case #2

Thermal effects: bending moments M_x



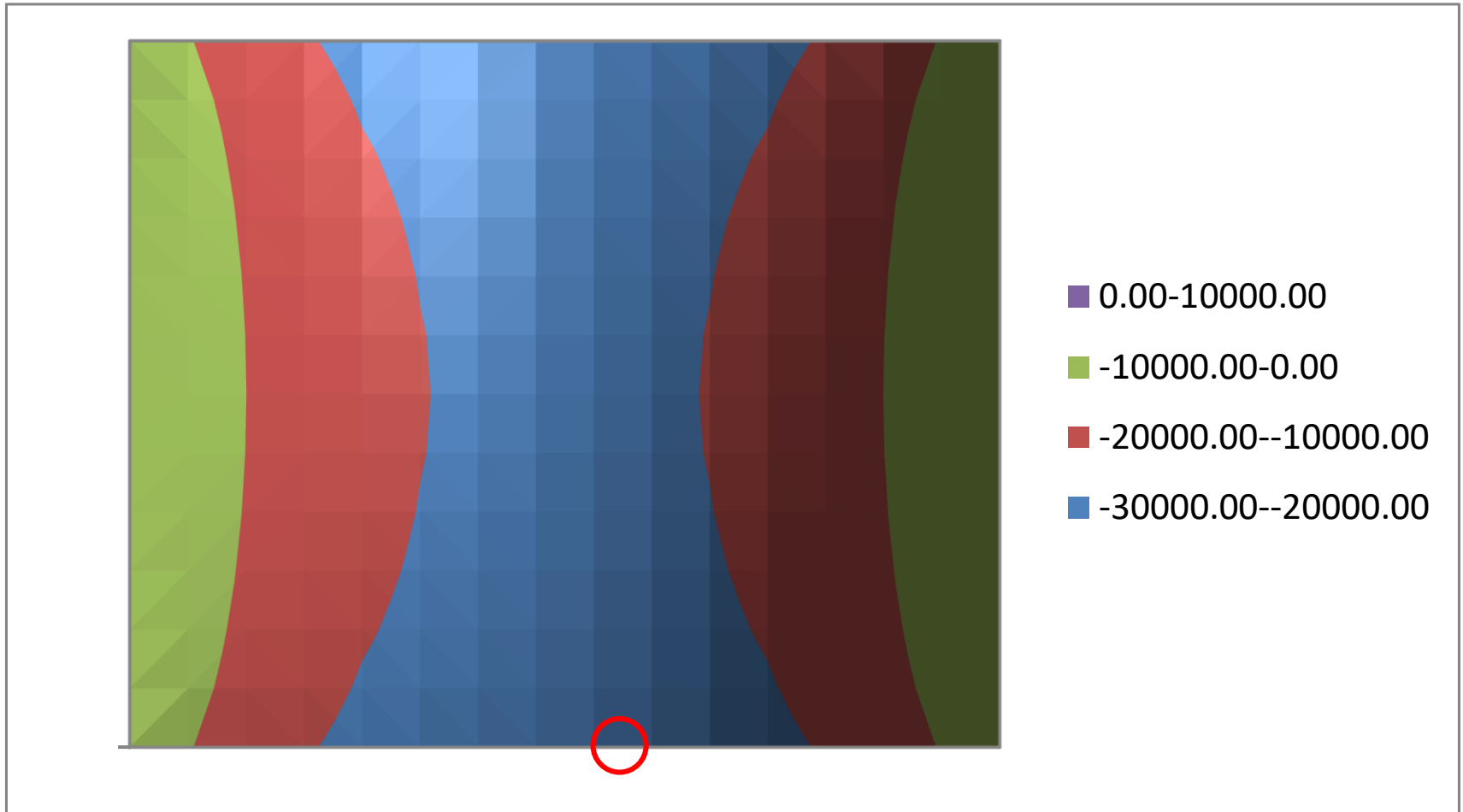
- 0.00-5000.00
- 5000.00-0.00
- 10000.00--5000.00
- 15000.00--10000.00



$M_{x,max} = 8865.89 \text{ Nmm/mm}$

Case #2

Thermal effects: maximum tensile stresses σ_x



$$\sigma_{s,\max} = \frac{6 \cdot M_{x,\max}}{s^2} = \frac{6 \cdot 25930.50}{250^2} = 2.48 \text{ MPa}$$

Case #2

Load Combination: displacements

E=	27586	MPa	Self-weight multiplier		Center-point force		Thermal effects			
s=	250	mm	$\gamma_g =$	1.00	F=	40.00	kN	$\Delta t =$	-10	°C
v=	0.2		g=	6.25	kN/m ²			$\alpha_c =$	1.20E-05	°C ⁻¹
$\gamma =$	25.0	kN/m ³						$\chi^* =$	4.80E-07	mm ⁻¹
D=	3.742E+10	Nmm								
$k_0 =$	0.04073	N/mm ³								
$L_x =$	5000	mm								
$L_y =$	5000	mm								
n=	10									
$\Delta =$	304.8	mm								

The figure is a 3D surface plot representing displacement contours. The vertical axis (z-axis) is labeled with values from -0.20 to 0.40 in increments of 0.10. The horizontal axes represent the spatial dimensions of the structure. The surface shows a complex shape with a central peak at approximately -0.15 and a larger peak at approximately 0.35. The surface is colored with a gradient from blue (low displacement) to red (high displacement). The plot is enclosed in a 3D wireframe box.

The End

Thank you for your attention